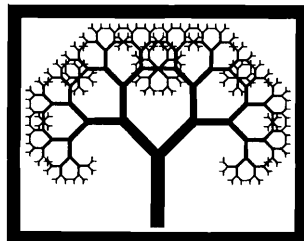


**ADVANCES  
IN  
FINITE ELEMENT  
TECHNOLOGY**



**ADVANCES  
IN  
FINITE ELEMENT  
TECHNOLOGY**

*Edited by  
B.H.V. Topping*



**CIVIL-COMP PRESS**

**CIVIL-COMP PRESS**  
**10 Saxe-Coburg Place**  
**Edinburgh, EH3 5BR, UK**

*CIVIL-COMP PRESS is an imprint of Civil-Comp Limited*

© 1996, *Civil-Comp Limited*

**British Library Cataloguing in Publication Data**

A catalogue record for this book is available from the British Library

ISBN 0-948749-41-5

Printed in the Scottish Borders  
by  
MEIGLE PRINTERS LIMITED  
Galashiels, Scotland

# ❖CONTENTS❖

## 1. MESH GENERATION AND GEOMETRIC REPRESENTATION

- 1.1 A REVIEW OF MESH GENERATION, N.P. Weatherill, Department of Civil Engineering, University of Wales, Swansea, United Kingdom ..... 1
- 1.2 DERIVATION OF APPROPRIATE IDEALISATIONS IN FINITE ELEMENT MODELLING, C.G. Armstrong, R.J. Donaghy and S.J. Bridgett, Department of Mechanical and Manufacturing Engineering, The Queen's University of Belfast, Belfast, United Kingdom ..... 11
- 1.3 THREE DIMENSIONAL GEOMETRIC MODELLING BASED ON NURBS: A REVIEW, E. Dimas\* and D. Briassoulis#, \*Catholic University of Leuven, Leuven, Belgium, #Department of Agricultural Engineering, Agricultural University of Athens, Athens, Greece ..... 21
- 1.4 FLOW MODELLING USING QUADTREES AND MULTIGRID TECHNIQUES, C. Gaspar, Department of Mathematics, Szechenyi Istvan College, Gyor, Hungary ..... 31

## 2. ADAPTIVITY AND ERROR ESTIMATORS

- 2.1 IMPROVED EIGENFREQUENCIES AND EIGENMODES IN FREE VIBRATION ANALYSIS, N.-E. Wiberg, R. Bausys and P. Hager, Department of Structural Mechanics, Chalmers University of Technology, Goteborg, Sweden..... 43
- 2.2 A POSTERIORI ERROR ESTIMATION IN CONSTITUTIVE LAW FOR ACOUSTIC FINITE ELEMENT ANALYSIS, P. Bouillard and G. Warzee, Department of Continuum Mechanics, Universite Libre de Bruxelles, Brussels, Belgium. .... 55
- 2.3 ASPECTS OF HIERARCHICAL h-ADAPTIVE DYNAMIC ANALYSES, J. Riccius and K. Schweizerhof, Institute for Mechanics, University of Karlsruhe, Karlsruhe, Germany ..... 61
- 2.4 AN ADAPTIVE MULTIGRID ALGORITHM FOR FINITE ELEMENT ANALYSIS OF PLATES, S. Lopez\* and S. Fortino#, \*Institute of Construction Science, University of Bologna, Bologna, Italy, #Department of Structures, University of Calabria, Italy..... 71
- 2.5 ADAPTIVE CONTROL FOR TIME-DEPENDENT NONLINEAR FINITE ELEMENT ANALYSIS, P. Ladeveze and N. Moes, Laboratory of Mechanics and Technology, ENS Cachan/University of Paris, France ..... 79
- 2.6 QUASI-REGIONAL MAPPING FOR THE P-VERSION OF THE FINITE ELEMENT METHOD, Gy. Kiralyfalvi and B.A. Szabo, Center for Computational Mechanics, Washington University, St. Louis, United States of America..... 93
- 2.7 POLYNOMIAL REPRESENTATIONS WITH BUILT-IN FIELD EQUATIONS FOR PATCH RECOVERY PROCEDURES, J. Aalto and M. Aman, Department of Civil Engineering, University of Oulu, Oulu, Finland.....109
- 2.8 DISPLACEMENT BASED CONTINUOUS STRESS RECOVERY PROCEDURE, D. Mijuca\*, Z. Draskovic# and M. Berkovic\*,\*Faculty of Mathematics, Belgrade, Yugoslavia, #Mathematical Institute, Belgrade, Yugoslavia..... 127
- 2.9 BUILT-IN FIELD EQUATIONS FOR PATCH RECOVERY PROCEDURES USING WEIGHTED RESIDUALS, J. Aalto and M. Perala, Department of Civil Engineering, University of Oulu, Oulu, Finland .....135
- 2.10 A HIERARCHICAL ADAPTIVE FINITE ELEMENT STRATEGY FOR ELASTIC-PLASTIC PROBLEMS, H. Cramer, M. Rudolph, G. Steinl and W. Wunderlich, Technical University of Munich, Munich, Germany .....151

- 2.11 THE ANALYSIS AND DESIGN OF STIFFENED SHELL STRUCTURES USING AUTOMATIC ADAPTIVE MESH GENERATION AND ERROR ESTIMATORS, J.W. Bull\*, L.Y. Li\* and P. Bettess\* and T. Bond#, \*Engineering Design Centre, University of Newcastle upon Tyne, Newcastle upon Tyne, United Kingdom, #Department of Mechanical Engineering and Manufacturing Systems, University of Northumbria at Newcastle, Newcastle upon Tyne, United Kingdom ..... 161
- 2.12 NONLINEAR ADAPTIVE ANALYSIS AND ANIMATION VIA QUASI-NEWTON APPROACH, O. Ohtmer, Department of Mechanical Engineering, California State University, Long Beach, United States of America ..... 167

### 3. ELEMENT TECHNOLOGY

- 3.1 NUMERICAL IMPLEMENTATION OF HYBRID-TREFFTZ DISPLACEMENT ELEMENTS, J.A. Teixeira de Freitas and C. Cismasiu, Department of Civil Engineering, I.S.T., Technical University of Lisbon, Lisbon, Portugal ..... 179
- 3.2 UNIVERSAL SERENDIPITY ELEMENTS WITH UNEQUALLY SPACED EDGE NODES, M. Utku, Department of Civil Engineering, Middle East Technical University, Ankara, Turkey ..... 189
- 3.3 FORMULATION OF HYBRID-TREFFTZ DISPLACEMENT ELEMENTS, J.A. Teixeira de Freitas and C. Cismasiu, Department of Civil Engineering, I.S.T., Technical University of Lisbon, Lisbon, Portugal ..... 195

### 4. FINITE ANALYSIS OF PLATE AND SHELL STRUCTURES

- 4.1 EFFICIENT 3-NODE SHEAR DEFORMABLE PLATE/SHELL ELEMENTS - AN ALMOST HOPELESS UNDERTAKING, C. Hausser and E. Ramm, University of Stuttgart, Stuttgart, Germany ..... 203
- 4.2 A SURVEY IN THE DEFINITION OF TRANSVERSE DISPLACEMENT FOR DISCRETE REISSNER-MINDLIN PLATE ELEMENTS, R.M. Sydenstricker and L. Landau, Department of Civil Engineering, COPPE/UFRJ Federal University of Rio de Janeiro, Rio de Janeiro, Brazil ..... 217
- 4.3 A SUPER-B-SPLINE FINITE ELEMENT METHOD FOR BUCKLING AND VIBRATION ANALYSIS OF PLATES, S. Wang, School of Civil Engineering, The University of Birmingham, Birmingham, United Kingdom ..... 231
- 4.4 MODELLING GENERAL SHELL CONFIGURATIONS WITH A FOUR-NODE SHELL ELEMENT, D. Briassoulis, Department of Agricultural Engineering, Agricultural University of Athens, Athens, Greece ..... 237

### 5. TECHNIQUES FOR THE SOLUTION OF LARGE SCALE PROBLEMS

- 5.1 A GRAPH THEORETICAL METHOD FOR FRONTWIDTH REDUCTION, A. Kaveh\* and G.R. Roosta#, \*Iran University of Science and Technology, Tehran, Iran, #Building and Housing Research Centre, Tehran, Iran ..... 245
- 5.2 A UNIFIED SET OF ALGORITHMS FOR PROFILE AND WAVEFRONT REDUCTION OF SPARSE MATRICES WITH A SYMMETRIC STRUCTURE, S.R.P. Medeiros, P.M. Pimenta, P. Goldenberg and R.M.L.R.F. Brasil, Department of Structural and Foundation Engineering, University of Sao Paulo, Sao Paulo, Brazil ..... 255
- 5.3 BANDWIDTH OPTIMIZATION FOR RECTANGULAR MATRICES, A. Kaveh and A. Mokhtar-zadeh, Iran University of Science and Technology, Tehran, Iran ..... 263
- 5.4 FAST ITERATIVE SOLVERS FOR FINITE ELEMENT ANALYSIS IN GENERAL AND SHELL ANALYSIS IN PARTICULAR, P. Saint-Georges, G. Warzee, Y. Notay and R. Beauwens, Service des Milieux Continus & Service de Metrologie Nucleaire, Universite Libre de Bruxelles, Bruxelles, Belgium ..... 273

## **6. FINITE ELEMENT MODELLING OF GEOTECHNICAL AND GEOMECHANIC PROBLEMS**

- 6.1 ANALYSIS OF DISCONTINUITIES IN GEOMECHANICS WITH JOINT ELEMENTS, M.H.F. Melao Barros and M. Eugenia Rocha, Civil Engineering Department, Faculty of Sciences and Technology, Coimbra, Portugal.....283
- 6.2 DAMPING OF TUBES FILLED WITH GRANULAR MATERIALS: A NON-CONSERVATIVE DYNAMIC STIFFNESS ANALYSIS, J.M. Bourinet and D. Le Houedec, Laboratory of Mechanics and Materials, Ecole Centrale de Nantes, Nantes, France.....289
- 6.3 FINITE ELEMENT ANALYSES OF VERTICAL ANCHOR WALL BEHAVIOUR IN CLAY BACKFILL, E.A. Dickin and G.J.W. King, Department of Civil Engineering, The University of Liverpool, Liverpool, United Kingdom .....301

## **7. NON-LINEAR SOLUTION AND TRANSIENT DYNAMIC SOLUTION PROCEDURES**

- 7.1 A LARGE TIME INCREMENT APPROACH FOR THERMO-MECHANICAL PROBLEMS, J.Y. Cognard, P. Ladeveze and P. Talbot, Laboratory of Mechanics and Technology, ENS Cachan/University of Paris, France...309

## **8. MATERIALS MODELLING**

- 8.1 RATE-DEPENDENT SMEARED CRACK MODEL IN TRANSIENT DYNAMIC ANALYSES, Z. Ren\* and N. Bicanic#, \*Faculty of Mechanical Engineering, University of Maribor, Maribor, Slovenia, #Department of Civil Engineering, University of Glasgow, Glasgow, United Kingdom .....319
- 8.2 NUMERICAL ANALYSIS OF THE PLAIN CONCRETE MODEL PREDICTION FOR NONPROPORTIONAL LOADING PATHS, A. Winnicki and Cz. Cichon, Cracow University of Technology, Cracow, Poland .....331
- 8.3 THE BIPOTENTIAL APPROACH: SOME APPLICATIONS, M. Hjjaj\*, G. De Saxce# and N.-E. Abriak\*, \*School of Mines of Douai, Douai, France, #LML, University of Lille, Lille, France.....341

## **9. FINITE ELEMENT STUDIES FOR ANALYSIS, DESIGN AND MAINTENANCE**

- 9.1 THE NUMERICAL MODELLING OF CAMOUFLETS TO DETERMINE THEIR EFFECT ON OVERLAYING RUNWAYS, J.W. Bull\* and C.H. Woodford#, \*Department of Civil Engineering and #Computing Service, The University, Newcastle upon Tyne, United Kingdom .....349
- 9.2 FINITE ELEMENT ANALYSIS FOR SEISMIC DAMAGE PREDICTION OF A RETROFITTED MASONRY BUILDING, M.A. Haroun, H. Bhatia and E.H. Ghoneam, Department of Civil and Environmental Engineering, University of California, Irvine, United States of America .....357
- 9.3 VIBRATION OF VARYING THICKNESS CIRCULAR CYLINDERS UNDER UNIFORM EXTERNAL PRESSURE, C.T.F. Ross, M.W. Taylor and W.D. Richards, Department of Mechanical & Manufacturing Engineering, University of Portsmouth, Portsmouth, United Kingdom .....363
- 9.4 SIMPLIFIED PROCEDURE FOR THE NONLINEAR SEISMIC ANALYSIS OF BRIDGES, F. Montans and E. Alarcon, Department of Structural Mechanics and Industrial Constructions, Technical University of Madrid, Madrid, Spain .....371
- 9.5 DESIGN OF A VIBRATION ISOLATING SCREEN, G. De Roeck\*, G. Degrande\*, W. Dewulf\*, P. Van de Broeck\* and M. Verlinden#, \*Department of Civil Engineering, Catholic University of Leuven, Heverlee, Belgium, #ICOS Benelux, Brussels, Belgium.....379
- 9.6 NONLINEAR ANALYSIS FOR THE DESIGN OF RC PLATES AND SHELLS, U. Wittek and R. Meiswinkel, Department of Statics, University of Kaiserslautern, Kaiserslautern, Germany .....387

9.7 THE MODELLING OF CONTINUOUS CONCRETE SURFACING OVERLAYING THE REPAIR OF CRATERS IN AIRFIELD RUNWAYS, J.W. Bull* and C.H. Woodford#, *Department of Civil Engineering and #Computing Service, The University, Newcastle upon Tyne, United Kingdom .....	395
9.8 BMM FOR LONG-TERM BRIDGE DETERIORATION BY DYNAMIC STRUCTURAL ANALYSIS SYSTEM, H. Alaylioglu and A. Alaylioglu, GPG - Structures, Pretoria, South Africa .....	405
9.9 NEUTRAL AXIS VARIATION IN BRIDGE DECKS, E.J. O'Brien and D.L. Keogh, Department of Civil, Structural and Environmental Engineering, Trinity College, Dublin, Ireland.....	421
9.10 FINITE ELEMENT MODELLING OF DRIVEN NOTCH BEHAVIOUR IN POLYMER, Z.W. Guan, Department of Civil Engineering, University of Brighton, Brighton, United Kingdom.....	429
9.11 COLLAPSE OF THICK-WALLED CIRCULAR CONICAL SHELLS UNDER EXTERNAL PRESSURE, C.T.F. Ross and D. Sawkins, Department of Mechanical and Manufacturing Engineering, University of Portsmouth, Portsmouth, United Kingdom .....	437
 <b>10. VISUALISATION OF THE FINITE ELEMENT METHOD</b>	
10.1 VISUALIZATION OF FE-DATA, INTERACTIVELY AND ON VIDEO, H. Tagnfors, Department of Structural Mechanics, Chalmers University of Technology, Goteborg, Sweden .....	443



## ❖PREFACE❖

This volume contains a selection of papers presented at *The Third International Conference in Computational Structures Technology*, held in Budapest from 21st August-23rd August 1996. The papers in this volume include the following topics: Mesh Generation and Geometric Representation; Adaptivity and Error Estimators; Element Technology; Finite Element Analysis of Plate and Shell Structures; Solution of Large Scale Problems; Finite Element Modelling of Geotechnical and Geomechanic Problems; Materials Modelling; Finite Element Studies for Analysis, Design and Maintenance; and Visualisation of the Finite Element Method. Other papers from the conference are published in:

- Advances in Computational Structures Technology  
Civil-Comp Press, 1996, ISBN 0-948749-40-7
- Advances in Optimization for Structural Engineering  
Civil-Comp Press, 1996, ISBN 0-948749-42-3
- Advances in Analysis and Design of Composites  
Civil-Comp Press, 1996, ISBN 0-948749-43-1
- Advances in Computational Methods for Simulation  
Civil-Comp Press, 1996, ISBN 0-948749-44-X
- Advances in Computational Techniques for Structural Engineering  
Civil-Comp Press, 1996, ISBN 0-948749-45-8
- Advances in Boundary Element Methods  
Civil-Comp Press, 1996, ISBN 0-948749-46-6

I am grateful to Professor N.P. Weatherill (University of Wales, Swansea, UK) and Professor E. Ramm (University of Stuttgart, Germany) whose special lectures are included in this volume.

I should like to thank all the authors for their contributions and in particular those who presented their papers in Budapest. I must also thank the members of the Conference Editorial Board who helped in many ways before and during the conference. The members of the Editorial Board for Computational Structures Technology Conference 1996, were: Professor H. Adeli, USA, Professor N. Akkas, Turkey, Professor E. Alarcon, Spain, Professor J. Argyris, Germany, Professor O. Axelsson, The Netherlands, Professor K.J. Bathe, USA, Dr L. Berke, USA, Professor H.J.C. Barbosa, Brazil, Professor J.W. Baugh, USA, Professor T. Belytschko, USA, Professor P.G. Bergan, Norway, Professor D. Beskos, Greece, Professor P. Bettles, UK, Professor N. Bicanic, UK, Professor R.I. Borja, USA, Professor F. Brezzi, Italy, Dr John W. Bull, UK, Professor C. Cingini, Italy, Dr. A.H.C. Chan, UK, Professor I. St Doltsinis, Germany, Professor I.S. Duff, UK and France, Dr L. Dunai, Hungary, Professor A. Eriksson, Sweden, Professor D. Frangopol, USA, Professor J.A. Teixeira de Freitas, Portugal, Professor F. Frey, Switzerland, Professor R. Fruchter, USA, Professor M.B. Fuchs, Israel, Professor G. Gambolati, Italy, Professor M. Geradin, Belgium, Professor D.E. Grierson, Canada, Professor D. Hartmann, Germany, Professor P. Hajela, USA, Professor E. Hinton, UK, Professor M.A. Hogge, Belgium, Professor T.J.R. Hughes, USA, Professor M. Ivanyi, Hungary, Professor W.M. Jenkins, UK, Dr P.K. Jimack, UK, Professor S. Kaliszky, Hungary, Professor D.I. Karabalis, USA, Professor A. Kaveh, Iran, T. Kenny, UK, Dr A.I. Khan, Australia, Professor N. Kikuchi, USA, Professor U. Kirsch, Israel, Professor Dr M. Kleiber, Poland, Professor V.K. Koumoussis, Greece, Professor W.B. Kratzig, Germany, Professor P. Ladeveze, France, Professor K.L. Lawrence, USA, Dr. S.H. Lee, USA, Professor P. Leger, Canada, Professor A.Y.T. Leung, Hong Kong, Dr. R. Levy, Israel, Professor A. Liolios, Greece, Professor W.K. Liu, USA, J. Mackerle, Sweden, Professor G. Maier, Italy, Professor J. Mandel, USA, Professor H.A. Mang, Austria, Professor I.M. May, UK, Dr J.J. McKeown, UK, Professor J.L. Meek, Australia, Dr H.P. Mlejnek, Germany, Professor G. Molnarka, Hungary, Professor C.A. Mota Soares, Portugal, Dr D.T. Nguyen, USA, Professor A. K. Noor, USA, Professor R. Ohayon, France, Professor E. Onate, Spain, Dr K. Orsborn, Sweden, Professor D.R.J. Owen, UK, Professor M. Papadrakakis, Greece, Professor P.Y. Papalambros, USA, Professor K.C. Park, USA, Professor D. Parsons, USA, Dr. M.N. Pavlovic, UK, Professor M.S. Pereira, Portugal, Dr V.K. Peshkam, UK, Professor E. Ramm, Germany, Professor F. Rammerstorfer, Austria, Professor G. De Roeck, Belgium, Professor A. Samartin, Spain, Professor B. Schrefler, Italy, Professor K. Sweitzerhof, Germany, Dr. G.M. Seed, UK, Professor N. Schirraishi, Japan, Dr. H.D. Simon, USA, Professor G.S. Springer, USA, Dr. I. Sobieski, USA, Professor K.S. Surana, USA, Professor C.A. Symakezis, Greece, Professor B.A. Szabo, USA, Professor R. Szilard, USA, Professor G Thierauf, Germany, Dr G. Turvey, UK, Professor Y. Ueda, Japan, Dr G. Vanderplaats, USA, Dr V.B. Venkayya, USA, Professor K.S. Virdi, UK, Professor Z. Waszczyszyn, Poland, Professor N.P. Weatherill, UK, Professor N-E Wiberg, Sweden, Professor J.P. Wolf, Switzerland, Professor W. Wunderlich, Germany, Professor Yong Bin Yang, Taiwan, and Dr. Th. Zimmermann, Switzerland.

The idea of holding the Third International Conference on Computational Structures Technology in Budapest came from János Sziveri, Heriot-Watt University, Edinburgh. I should like to thank him for his help, advice and support over the two year period before this conference. My thanks are also due to all at Civil-Comp Press for their help and

perseverance in the realisation of this conference, particularly Szandra Köves and Maisie Sales. The assistance of members of the Structural Engineering Computational Technology Research Group at Heriot-Watt University, Edinburgh is gratefully acknowledged particularly from Péter Iványi, Biao Cheng, Ardeshir Bahreininejad, Joao P.B. Leite and Janet Wilson.

Barry Topping  
Department of Mechanical and Chemical Engineering  
Heriot-Watt University, Edinburgh  
August 1996